# Mathematical Analysis and Systems Theory

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# Mathematical Systems Theory and Control



Mathematical control theory studies differential equations

$$\frac{d}{dt}x(t) = Ax(t) + Bu(t), \qquad x(0) = x_0$$
$$y(t) = Cx(t)$$

where

- $u(t) \in \mathbb{C}$  is the control input
- $y(t) \in \mathbb{C}$  is the measured output.

Key Focus Areas:

- Control of temperature and fluid flows
- Control of vibrating and flexible systems
- Dynamics of large-scale systems
- Modern mathematical techniques in control

# Example: Robust Trajectory Tracking for Heat Equations

Objective: Control the system in such a way that the temperature measurements converge to reference trajectories.



Figure: Controlled heat profile

Figure: Measurements

# Example: Optimal Disturbance Rejection

Objective: Choose locations of active dampers so that the structural vibrations are suppressed as efficiently as possible.



### Example: Dynamics of Large Vehicle Formations



Source: Ploeg et. al., '11.



#### Source: TED/R. D'Andrea

# Research Group at TUT

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